

## Proportions and ratios, Fractions and Decimals

NPD Stages	Operational domains (Strategy)	NUMICON	Numicon Milestone points
Stage 1 (one to one counting)	I am trying to make my sets the same.	<b>Firm Foundations</b> <b>Breaking Barriers</b> Pattern and Algebra 6 NNS 2, 20 Cal 6 <b>Numicon 1</b> NPC SF2	Same and different Matching
Stage 2 (counting from 1 on materials)	I can share equally using materials.	<b>Firm Foundations</b>  <b>Breaking Barriers</b> Cal 16, 17 <b>Numicon 2</b> Numicon 1 NPC CAL 5	Doubles and halves
Stage 3 (Counting from 1 by imaging)	I can divide a region into equal parts using materials. I can share equally using materials or imaging.		
Stage 4 (advanced counting)	I can divide a region into equal parts using materials or imaging. -I can share equally using materials or imaging.		I know that 'half' means one of two equal parts of an object, shape or quantity
Stage 5 (early additive)	-I can find a fraction of a number.	<b>Breaking Barriers</b> Cal 18  <b>Numicon 2</b> Numicon 2 NNS 6  Numicon 2 CAL 15, 16	I know that 'quarter' means one of four equal parts of an object, shape or quantity I can read, recognize, find and write and explain that fractions are between whole numbers on the number line fractions of a number. $\frac{1}{2}$ , $\frac{1}{4}$ , $\frac{1}{3}$ , $\frac{3}{4}$ I can explain equivalence between $\frac{1}{2}$ and $\frac{2}{4}$ I understand $\frac{3}{4}$ as three of four equal parts I can divide 'How many...in...?'
	-I can solve division problems with remainders in my head using halving or what I know about basic facts.	<b>Numicon 3</b> Numicon 3 NNS 7, 8 Numicon 3 CAL 7, 11, 15, 16	I can solve problems with fractions of a whole and fractions as numbers I can use fraction notation to describe parts of a discrete set I can interpret a remainder as what is left after grouping I can use dividing to solve problems with sharing, knowing that there can be remainders in sharing situations
Stage 6 (Advanced Additive-)	-I can use repeated halving or known multiplication and division facts to solve	<b>Numicon 4</b>	I can: -recognise and show, using diagrams, families of common

Early Multiplicative)	<p>problems.</p> <ul style="list-style-type: none"> <li>-I can find fractions of a set or region.</li> <li>-I can rename improper fractions.</li> <li>-I can solve division problems that have remainders.</li> <li>-I can use simple repeated multiplication to solve simple problems involving ratios and rates.</li> </ul>		<p>equivalent fractions</p> <ul style="list-style-type: none"> <li>-count up and down in hundredths; recognise that hundredths arise when dividing an object by 100 and dividing tenths by 10</li> <li>-solve problems involving fractions to calculate quantities, and fractions to divide quantities</li> <li>-add and subtract fractions with the same denominator</li> <li>-recognise and write decimal equivalents of any number of tenths or hundreds</li> <li>-recognise and write decimal equivalents to two places</li> <li>-find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths</li> <li>-round decimals with 1 decimal place to the nearest whole number</li> <li>-compare numbers up to 2 decimal places</li> <li>-solve simple measure and money problems involving fractions and decimals to 2 decimal places</li> <li>-use multiplication and division to solve problems involving ratios and rates.</li> </ul>
Stage 7	<p>I can:</p> <ul style="list-style-type: none"> <li>-Read decimals to three places</li> <li>-Identify symbols for any fraction, including tenths, hundredths, thousandths, and improper fractions, e.g., <math>\frac{56}{10}</math></li> <li>-Count forwards and backwards in halves, thirds, quarters, fifths, and tenths at least</li> <li>-Order unit fractions (top number of one) such as <math>\frac{1}{2}</math>, <math>\frac{1}{3}</math>, <math>\frac{1}{4}</math>, and <math>\frac{1}{5}</math></li> <li>-Say the decimal number word sequences forwards and backwards in tenths and hundredths.</li> <li>-Round decimals with up to two decimal places to the nearest whole number e.g., round 6.49 to 6, 19.91 to 20</li> <li>-Know tenths and hundredths in decimals to two places e.g., tenths in 7.2 is 72.</li> </ul>	<p><b>Numicon 5</b> NNS 2 and 3 Cal 1 and 2</p> <p>Cal 4</p>	<p>I can:</p> <ul style="list-style-type: none"> <li>-explain equivalences between improper fractions and mixed numbers</li> <li>-use my knowledge of factors and multiples to recognize and explain equivalences between proper fractions</li> <li>-recognize and explain decimal and common fraction equivalents</li> <li>- solving adding and subtracting number problems involving whole numbers up to 1000</li> <li>- solving adding and subtracting problems involving fractions and decimal fractions efficiently</li> <li>- round up decimals to two places and to the nearest whole number and to one decimal place</li> <li>- find the term-to-term rule for a linear sequence involving whole numbers, fractions and decimals and work out missing terms</li> <li>- use multiplying and dividing facts and knowledge of factors and multiples to solve problems</li> <li>- solve problems effectively by finding fractions of amounts, making use of multiplying and dividing facts</li> <li>- use knowledge of factors and multiples to find equivalent</li> </ul>

		NNS 6 and Cal 7	<p>fractions and to simplify fractions to their lowest terms.</p> <ul style="list-style-type: none"> <li>- compare and order fractions with denominators which are multiples of the same number</li> <li>- use column algorithms to solve problems of + - x and ÷ with whole numbers and up to 3 decimal places</li> <li>- use multiplying facts to x and ÷ whole numbers and decimals by 10, 100, and 1000</li> <li>- calculate with powers of 10 to solve problems of x and ÷</li> <li>- use x and ÷ to solve problems involving scaling</li> <li>- explain percentage as the number of parts per hundred</li> <li>- find and explain percentage, fraction and decimal equivalents in order to solve problems in context.</li> </ul>
Stage 8	<p>I can:</p> <ul style="list-style-type: none"> <li>-Recall fraction ↔ decimal ↔ percentage conversions for given fractions and decimals</li> <li>-Know the number of tenths, hundredths, that are in numbers of up to three decimal places e.g., there are 456 tenths in 45.6</li> <li>-Know what happen when a whole number or decimal is multiplied or divided by a power of 10, e.g., <math>4.5 \times 100 = 450</math></li> <li>-Round decimals to the nearest hundred, ten, one, one-tenth, or one-hundredth.</li> <li>-Say the number one-thousandth, one-hundredth, one-tenth, one, ten, etc. before and after any decimal number</li> <li>-Order fractions, decimals, and percentages</li> </ul>		<p>I can:</p> <ul style="list-style-type: none"> <li>-use common factors to simplify fractions; use common multiples to express fractions in the same denomination</li> <li>compare and order fractions, including fractions &gt; 1</li> <li>-add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions</li> <li>-multiply simple pairs of proper fractions, writing the answer in its simplest form</li> <li>-divide proper fractions by whole numbers</li> <li>-associate a fraction with division and calculate decimal fraction equivalents for a simple fraction</li> <li>-identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places</li> <li>-multiply and divide up to two decimal places by whole numbers</li> <li>- rounding decimals to the nearest hundred, ten, one, one-tenth, or one-hundredth</li> <li>-recall and use equivalences between simple fractions, decimals and percentages</li> <li>-solve problems of two quantities where missing values can be found by using integer multiplication and division facts</li> <li>-solve problems involving the calculation of percentages and the use of percentages for comparison</li> <li>-solve problems involving similar shapes where the scale factor is known or can be found</li> <li>-solve problems involving unequal sharing and grouping using knowledge of fractions and multiples.</li> </ul>