

Progressions of Addition, Subtraction, Multiplication, Division and Algebra through NZC Phases 1 – 3 aligned with Numicon

Phase 1				
Must achieve during first 6 months	Must achieve during first year	Must achieve during second year	Progress outcomes by the end of the third year	Numicon
<ul style="list-style-type: none"> • join and separate groups of up to a total of 10 objects, and find the result by grouping and counting 	<p>recognise instantly the total number of objects in two patterns, each of up to five objects</p>	<ul style="list-style-type: none"> • partition a pattern of up to 10 objects, instantly recognise the number of objects in each part, and confirm the total number in the pattern using the parts 	<p>I know that: Numbers can be composed and decomposed in different ways by using patterns.</p>	Firm Foundations
	<ul style="list-style-type: none"> • partition and recombine sets of up to 10 in different ways • join and separate groups of up to a total of 20 objects, and find the difference between groups by grouping and counting 	<ul style="list-style-type: none"> • group, partition, and recombine whole numbers up to 100 • add and subtract numbers up to 100 by grouping and using number patterns 	<p>I know how to</p> <ul style="list-style-type: none"> • add and subtract two- and three-digit numbers 	Numicon 1
				Numicon 2
	<ul style="list-style-type: none"> • multiply and divide by making equal groups and using grouping or counting 	<ul style="list-style-type: none"> • multiply and divide by grouping and using number patterns 	<p>I know that: Multiplication and division involve recognising and working with groups, the number of groups, and the total.</p>	Firm Foundations
			<p>I know how to:</p> <ul style="list-style-type: none"> • multiply two single-digit numbers or multiply a single-digit and a two-digit number • divide whole numbers with a single-digit divisor and no remainders 	Numicon 1
				Numicon 2

<p>ALGEBRA</p> <ul style="list-style-type: none"> • copy, continue, create, and describe a repeating pattern with two elements 	<ul style="list-style-type: none"> • copy, continue, create, and describe a repeating pattern with three elements, and identify missing elements in a pattern 	<ul style="list-style-type: none"> • show that in an equation, both sides of the equal sign represent the same quantity • use both the unit of repeat and the ordinal position (e.g., first, second, and third) of a repeating pattern to predict further elements 	<p>I know that:</p> <p>The commutative property applies to addition (e.g., $2 + 5 = 5 + 2$) and multiplication (e.g., $5 \times 2 = 2 \times 5$). The additive identity is 0 (e.g., $4 + 0 = 4$ and $5 - 0 = 5$), and the multiplicative identity is 1 (e.g., $5 \times 1 = 5$ and $4 \div 1 = 4$).</p> <p>The equal sign is relational; it shows that the two sides of an equation are the same. Patterns are made of numeric or spatial elements in a sequence governed by a rule. Identifying the rule of a pattern involves working out the unit of repeat. An algorithm is a sequence of rules that can be followed.</p> <p>I know how to:</p> <ul style="list-style-type: none"> • recall addition facts to 20 and their corresponding subtraction facts • recall multiplication and corresponding division facts for twos, fives, and tens • solve true and false number sentences and open number sentences • use the additive and multiplicative identities and commutative property • find another element of a pattern, given part of it • describe a rule that explains how a pattern works • follow, and create patterns from, rules or simple algorithms. 	<p>Firm Foundations</p>
				<p>Numicon 1</p>
				<p>Numicon 2</p>
<p>Phase 2</p>				
<p>Must achieve during Year 4</p>	<p>Must achieve during Year 5</p>	<p>Progress outcomes by the end of Year 6</p>	<p>Numicon</p>	
<ul style="list-style-type: none"> • use their recalled addition and subtraction basic facts to solve problems 	<ul style="list-style-type: none"> • add and subtract whole numbers reliably and efficiently 		<p>Numicon 3</p>	

<ul style="list-style-type: none"> • add and subtract two- and three-digit numbers reliably and efficiently • add and subtract using the commutative property 			Numicon 4
<ul style="list-style-type: none"> • use the relationship between multiplication and division to divide • recall multiplication and corresponding division facts for threes and fours 	<ul style="list-style-type: none"> • multiply two-digit numbers using the distributive property • multiply reliably and efficiently • recall multiplication and corresponding division facts for sixes, eights, and nines 	<p>I know how to:</p> <ul style="list-style-type: none"> • add and subtract whole numbers and decimal numbers to two places • multiply two- and three-digit whole numbers • divide whole numbers by one- or two-digit divisors • find factors of numbers up to 100 	Numicon 5
<p>ALGEBRA</p> <ul style="list-style-type: none"> • solve addition and subtraction open number sentences using the relationship between the two sides of the equal sign 	<ul style="list-style-type: none"> • solve open number sentences involving all operations using the relationship between the two sides of the equal sign 	<p>I know that:</p> <p>The associative property applies to addition and multiplication (e.g., $3 \times (2 \times 7) = (3 \times 2) \times 7$).</p> <p>The distributive property applies to multiplication over addition and subtraction (e.g., $3 \times (10 + 7) = (3 \times 10) + (3 \times 7)$).</p>	Numicon 3
			Numicon 4
			Numicon 5
			Numicon 3

		<p>The equal (=) and inequality (<, >) signs show relationships.</p> <p>In a pattern, the relationship between the ordinal position (e.g., first, second, third) and the corresponding element is useful for finding the pattern rule.</p> <p>Tables and XY graphs provide a way of organising the positions and elements of a pattern to reveal relationships or rules.</p> <p>An algorithm is a set of instructions for solving a problem.</p> <p>I know how to:</p> <ul style="list-style-type: none"> • recall multiplication facts to 10×10 and corresponding division facts • use the distributive, commutative, and associative properties • solve open number sentences and true or false number sentences involving equality or inequality • use tables, XY graphs, and diagrams to find relationships between elements of growing patterns • develop a rule in words about a linear pattern • use a rule to make predictions • create and use algorithms for making decisions that involve clear choices. 	Numicon 4
Phase 3			Numicon 5
Progress outcomes by the end of Year 8			Numicon
<p>I know that:</p> <ul style="list-style-type: none"> • Multiplying a positive number by a number less than 1 results in an answer smaller than the original number. • Division can result in a remainder expressed as a whole number, fraction, or decimal. • Positive and negative numbers can be added and subtracted. 			Numicon 5

<p>I know how to:</p> <ul style="list-style-type: none"> • divide whole numbers reliably and efficiently • add and subtract decimals to three places • add and subtract fractions with the same denominator • multiply fractions and decimals by whole numbers • add and subtract integers. 	<p>Numicon 6</p>
<p>ALGEBRA</p> <p>I know that:</p> <p>The inverse property applies to addition (e.g., $3 + -3 = 0$) and multiplication (e.g., $3 \times \frac{1}{3} = 1$).</p> <p>Operations to both sides preserve the balance of an equation.</p> <p>The commutative, associative, distributive, and identity properties work the same for all numbers.</p> <p>A variable can be used to stand for any number.</p> <p>Functions are relationships or rules that uniquely associate members of one set with members of another set.</p> <p>Linear patterns and functions have a constant rate of change. They can be represented by ordered pairs, tables, XY graphs, and a rule (equation).</p> <p>Algorithms help solve problems in a systematic way. Their instructions are created, tested, and revised.</p> <p>I know how to:</p> <ul style="list-style-type: none"> • identify and describe the properties of prime, composite, and square numbers and the divisibility rules for 2, 3, 5, 9, and 10 • use words and symbols to describe and represent the properties of operations (commutative, distributive, associative, inverse, and identity) • solve linear equations by trial and improvement and by applying inverse operations • use variables to represent a rule about a linear pattern, and use the rule to make predictions • represent and connect linear functions using tables, equations, and XY graphs • create and use algorithms to identify, interpret, and explain patterns. 	<p>Numicon 5</p> <p>Numicon 6</p>